

COMPUTATIONAL INTELLIGENCE

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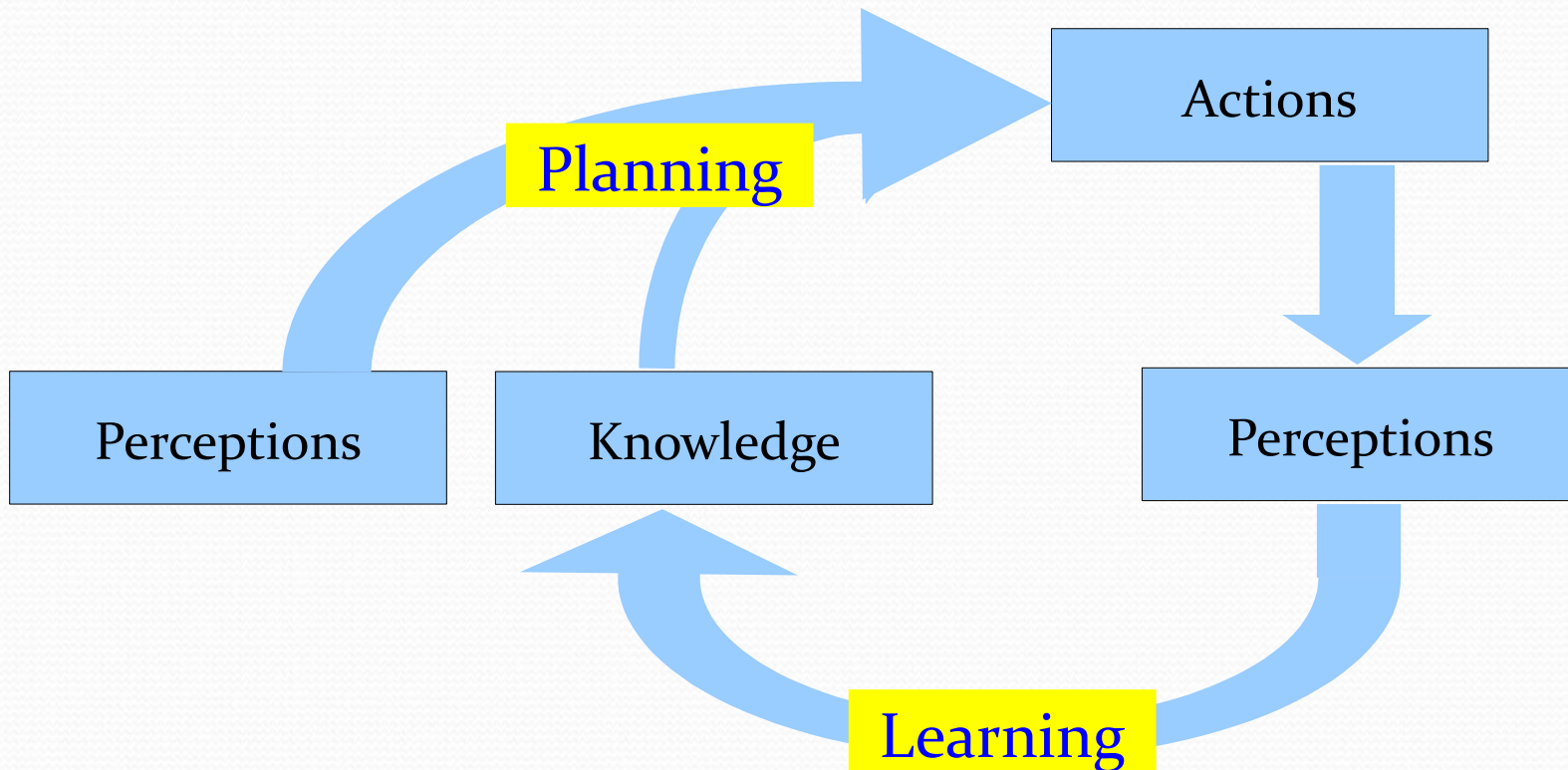
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Artificial Intelligence

- Aims to develop intelligent agents that perceive their environment and take actions that maximize their chances of success
- Requires solving several challenges:
 - Knowledge representation:
how does an agent represent its knowledge and perceptions?
 - Reasoning, planning:
how does an agent deduce an action based on its perceptions and its knowledge?
 - Learning:
how does an agent update its knowledge based on its perceptions?

Artificial Intelligence



Computational Intelligence

- Computational intelligence traditionally studies a subset of three AI techniques:
 - Knowledge representation:
fuzzy logic & fuzzy set theory
 - Reasoning, planning:
Evolutionary (genetic) algorithms
 - Learning:
Neural networks

Knowledge representation: Fuzzy logic

- **Goal:**
represent “fuzzy” knowledge of an agent
- Traditional logic can be used to represent crisp rules:

if A is true then do B

Boolean in → Boolean out

- Fuzzy logic represents fuzzy rules:

if A is true to a high degree / A is likely then try to make B true to a high degree / make B likely

Number in → Number out

Fuzzy logic is less sensitive to errors / noise

Knowledge representation: Fuzzy logic

- Used to build control systems

if A is warm to a high degree then B should be turned down to a high degree

- Used to calculate the overall quality (fitness) of a (hypothetical) situation

if A is high then customer is likely good

if B is high then customer is likely good

if C is high and B is not high then customer is likely good

how good would the situation be in which A and C are high, and B is low?

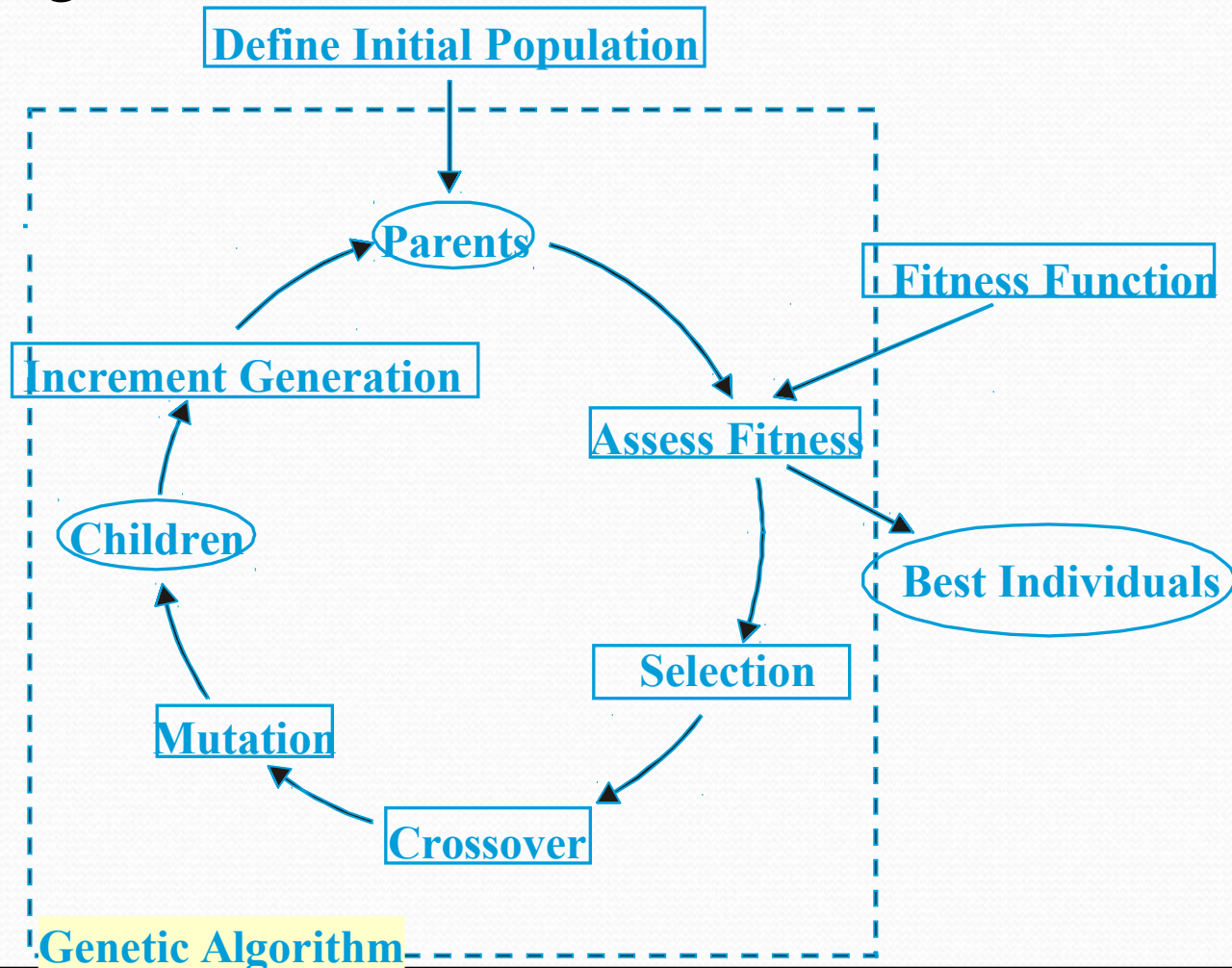
- ***Research challenges: how to interpret fuzzy rules? What are sensible strategies for calculating an output, given inputs? How to make the intuition formal?***

Planning / optimization: Evolutionary Algorithms

- **Goal of an evolutionary algorithm:**
to find a plan that optimizes a given fitness function
 - the fitness could be defined by means of fuzzy logic, but does not have to be
- **Example:**
the traveling salesman problem
 - **Given** a number of cities, distances between the cities
 - **Find** an order in which to visit the cities such that the total distance traveled is minimized

Evolutionary Algorithms

- **Method:** evolve populations of solutions by mimicking evolution in nature



Nature-inspired optimization

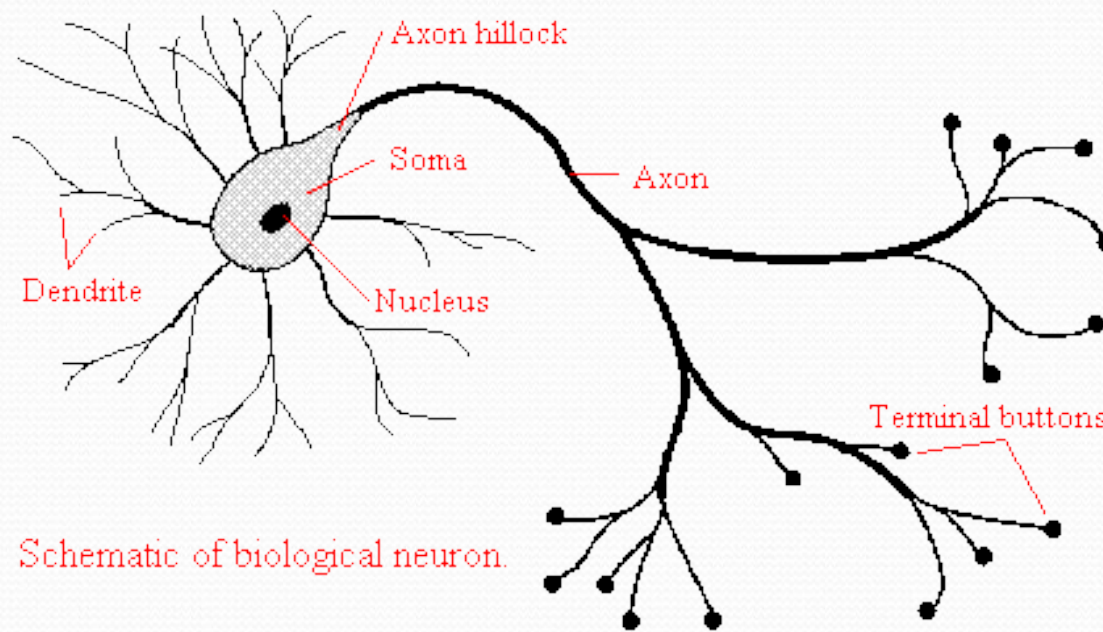
- Evolutionary algorithms
- Particle swarm optimization
- Artificial ants

**All are
robust optimization algorithms:
if the fitness function changes, solutions usually adapt
relatively easily**

- **Research challenge: which algorithm finds a good solution as quickly as possible?**

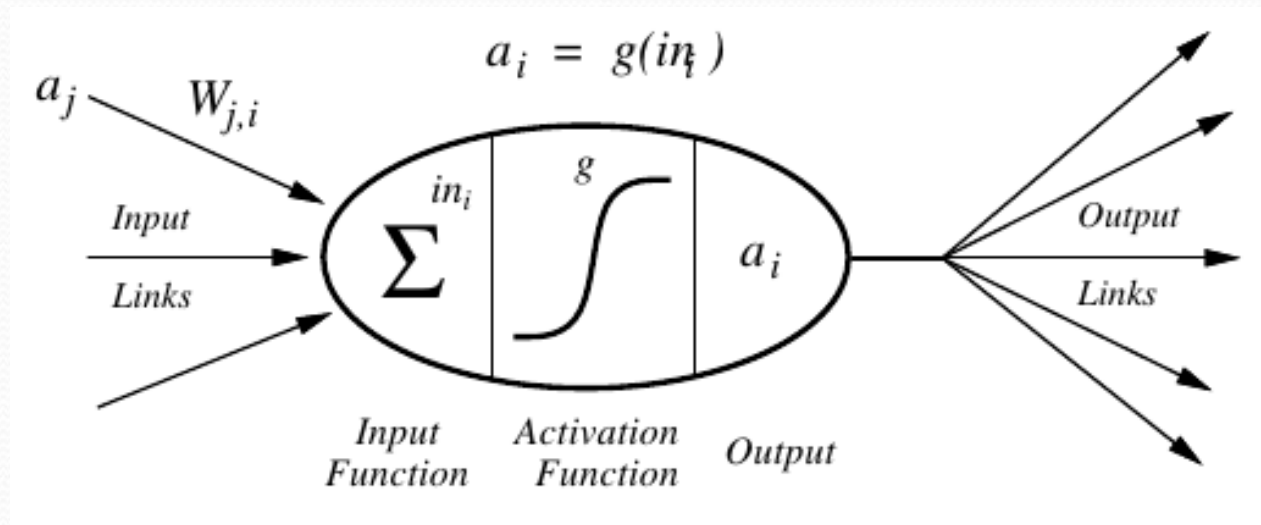
Learning: Neural Networks

- Inspired by biological nervous systems



Learning: Neural Networks

- Artificial neuron



(Neuron/Unit)

- Also a neural network represents knowledge, and is often used used to transform input to output

Learning:

Neural Networks

- Different types of neural networks:
 - feed-forward neural networks
 - self-organizing maps
 - recurrent networks
 - radial basis function networks
 - fuzzy-neural networks

**Research challenge: how to learn a neural network?
What is a good architecture for a neural network?**

Computational Intelligence

- Knowledge representation: fuzzy logic & fuzzy set theory → You haven't followed a basic course on logic
- Reasoning, planning: Evolutionary (genetic) algorithms
- Learning: Neural networks → Basis already discussed in course artificial intelligence
 - Also in course on data mining
 - Advanced topics require strong mathematics

● Knowledge representation & planning:
traditional logic, SAT solvers, constraint programming

Computational Intelligence

● Knowledge representation:
fuzzy logic & fuzzy set theory

● Reasoning, planning:
Evolutionary (genetic) algorithms

~~● Learning:
Neural networks~~

Central Theme

- Artificial intelligence inspired methods for
 - Knowledge representation:
 - Logic
 - Fuzzy logic
 - Optimization & planning:
 - SAT solving
 - Constraint programming
 - Local search
 - Evolutionary algorithms

Template of a Constraint Optimization Problem

- **Given:**
 - ...
- **Find:**
 - ...
- **Such that:**
 - ... is **minimal/maximal**
 - ... is satisfied

Example 1: Traveling Salesmen

- **Given:**

- N cities
- $D[i,j]$ distances between cities

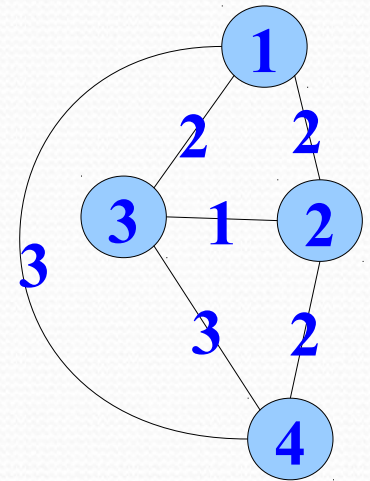
- **Find:**

- an assignment $p[i]$ for $i=1..N$ with $p[i]$ in $1..N$, indicating that at step i city $p[i]$ is visited

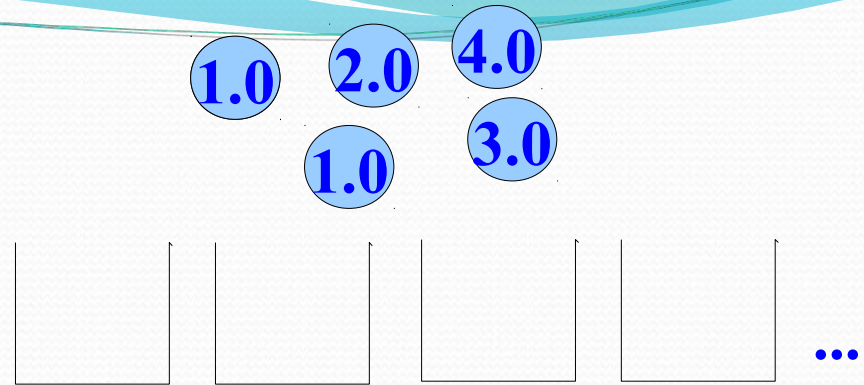
- **Such that:**

- all cities are visited exactly once
- $D[p[1],p[2]]+D[p[2],p[3]]+\dots+D[p[n-1],p[n]]+D[p[n],p[1]]$ is **minimal**

Optimization



Example 2: Binpacking



- **Given:**

- N items with sizes a_1, \dots, a_N
- A bin size V

Each bin: 4.0

- **Find:**

- an assignment $p[i]$ for $i=1..N$ to positive integers, indicating that item i is put in bin $p[i]$

- **Such that:**

- $\max_i p[i]$ is **minimal** (number of bins is small)
- $\sum_{p[i]=j} a_i \leq V$ for all bins j (no more than weight V in each bin)

Example 3: Knapsack

- **Given:**

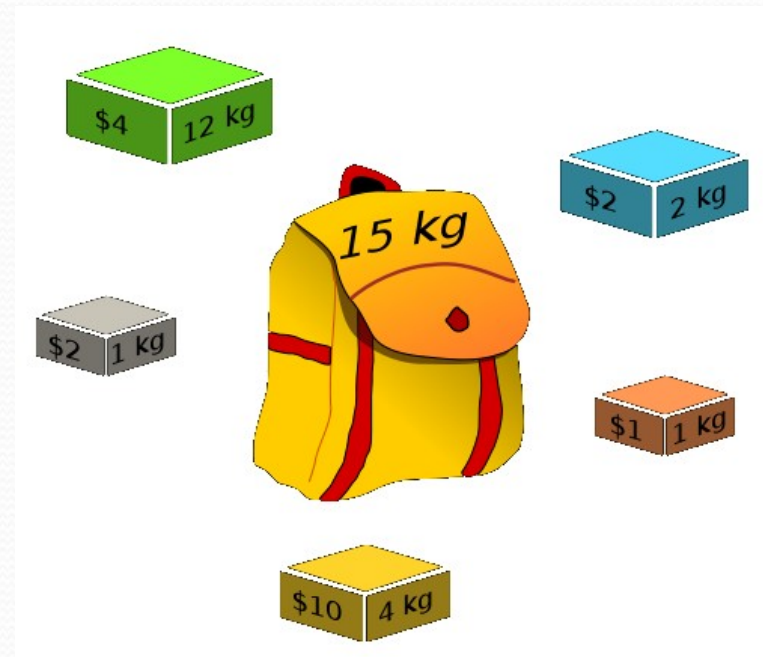
- N items with sizes a_1, \dots, a_N , prices p_1, \dots, p_N
- A maximum weight W

- **Find:**

- a subset of items I

- **Such that:**

- $\sum_{i \in I} p_i$ is **maximal** (very valuable knapsack)
- $\sum_{i \in I} a_i \leq W$ (knapsack with low weight)



Example 3b:

Unbounded Knapsack

- **Given:**

- N possible items with weights a_1, \dots, a_N , prices p_1, \dots, p_N
- A weight threshold W

- **Find:**

- an integer $w[i]$ for each item i

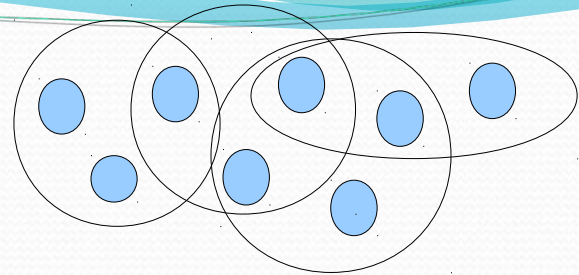
- **Such that:**

- $\sum_{i=1}^N w[i]p_i$ is **maximal** (very valuable knapsack)
- $\sum_{i=1}^N w[i]a_i \leq W$ (knapsack with low weight)

Portfolio
Optimization

Example 4:

Set Cover



- **Given:**

- N sets, each a subset of the universe $U = \{1, 2, \dots, m\}$

- **Find:**

- A subset S of the N given sets, i.e. each set in S equals one of the given sets, but not all given sets need to be selected.

- **Such that:**

- $|S|$ is **minimal** (small subset)

- $\bigcup_{S \in S} S = U$ (each element is covered)

Decision vs Optimization Problems

- Optimization problem:
 - Find ...
 - Such that:
 - $f(\dots)$ is minimal
 - constraints are satisfied
- Decision problem:
 - Find ...
 - Such that:
 - $f(\dots) < \textit{threshold}$
 - constraints are satisfied
- Optimization problems over finite domains can be turned into repeated decision problems: iterate over possible thresholds

How to solve these problems?

- Many such problems are hard
 - “NP hard” → no polynomial algorithm is known
- Two solutions:
 - Exact: require exponential time in the worst case
 - Inexact: polynomial, but may not find the best solutions
- Both types of solutions have been studied in artificial intelligence, algorithms, and operations research

High-Level, Declarative Problem Solving in AI

- Distinguishing feature of AI approaches: they aim to be “intelligent” and generic by solving problems (semi-)automatically
 - Idea: solve a problem in two stages:
 - 1. Describe the problem in a concise way in a computer language.
 - 2. Run a general algorithm (a “solver” or an “inference engine”) on this description to solve the problem.
- i.e., the programmer does **not** write an imperative algorithm.

High-Level Declarative Problem Solving in AI

- Example search: evolutionary algorithm
 - Step 1:
 - Specify what the individuals in a population look like
 - Specify the quality of an individual (fitness)
 - Step 2: (Ideal situation)
 - Run an existing evolutionary algorithm without modification



**Evolutionary
Algorithm**

Black box



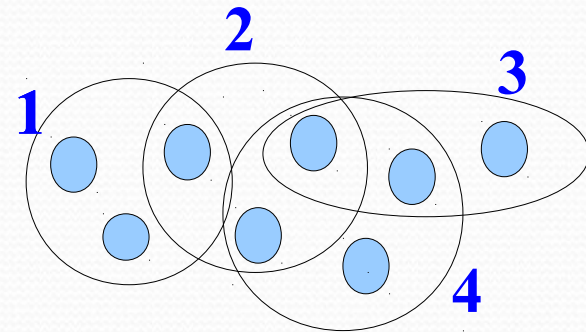
High-Level Declarative Problem Solving in AI

- Example problem: set cover
- Representation of an individual in a bitstring:



2nd and 3rd set are selected

- Fitness: (assuming small=very fit)
 - Number of sets selected?
 - Number of sets selected + (number of uncovered elements) $\times w$



Very large weight

High-Level Declarative Problem Solving in AI

- What about optimal solutions?
- Alternative *general* systems that take a *declarative* input specification and find optimal solutions:
 - Constraint programming
 - SAT solvers
 - ILP solver

High-Level Declarative Problem Solving in AI

- Which programming language to use?
 - C++ ?
 - Java ?
 - Prolog ?
 - Python

Why Python?

- Scripting language with a high level of abstraction
 - Implements features also seen in functional and logic programming
- Well-supported language with many libraries available
- Quickly gaining popularity in the scientific community (Coursera)

Why Python?

Language Rank	Types	2015 Spectrum Ranking	2014 Spectrum Ranking
1. Java	🌐 📱 🖥️	100.0	100.0
2. C	📱 🖥️ 🧠	99.9	99.3
3. C++	📱 🖥️ 🧠	99.4	95.5
4. Python	🌐 🖥️	96.5	93.5
5. C#	🌐 📱 🖥️	91.3	92.4
6. R	🖥️	84.8	84.8
7. PHP	🌐	84.5	84.5
8. JavaScript	🌐 📱	83.0	78.9
9. Ruby	🌐 🖥️	76.2	74.3
10. Matlab	🖥️	72.4	72.8

(IEEE Spectrum)

Computational Intelligence

- Basic course in Python
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- ~~● Learning:
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